Abstract: Data mining (also called knowledge discovery in databases) represents the process of extracting interesting and previously unknown knowledge (patterns) from data. By applying artificial intelligence together with analytical methods data can be extracted. An association rule expresses the dependence of a set of attribute-value pairs, called items, upon another set of items (item set). The association rule mining algorithms can be classified into two main groups: the level-wise algorithms and the tree-based algorithms. The level-wise algorithms scan the entire database multiple times but they have moderate memory requirement. The two phase algorithms scan the database only twice but they can have extremely large memory requirement. In this paper a comparative study of the algorithms used in association rules mining apriori and FP growth is done. A performance study has been done which shows the advantages and disadvantage of algorithms.

1. INTRODUCTION

The association rule mining is a fundamentally important task in the field of data mining. It is a process of discovering not trivial relationships between data in large databases. The problem of association rule mining was first introduced by Agrawal et al in 1993 [1]. Since then it is one of the most popular research area on the field of knowledge discovery.

The association rule mining problem is commonly known as the market basket analysis, but there are several applications that use association rules as well i.e. biological research areas, telecommunication and network analysis etc. Regarding the diversity of the applications that use association rule mining, several algorithms have been developed. All of these algorithms have their own advantages and disadvantages, so it is useful to compare them. Most of the algorithms find all frequent itemsets.

A very influential association rule mining algorithm, Apriori [1], has been developed for rule mining in large transaction databases. Many other algorithms developed are derivative and/or extensions of this algorithm. A major step forward in improving the performances of these algorithms was made by the introduction of a novel, compact data structure, referred to as frequent pattern tree, or FP-tree [2], and the associated mining algorithm, FP-growth. The main difference between the two approaches is that the Apriori-like techniques are based on bottom-up generation of frequent itemset combinations and the FPtree based ones are partition-based, divide-and-conquer methods.

After this introduction, the paper is organized as follows. Section 2 presents the problem definition. The main aspects of Apriori, FP-growth algorithms are presented in Section 3. Section 4 shows a comparative study of the algorithms and the paper is concluded in Section 5.

2. PROBLEM DEFINITION

Association rule mining finds interesting association or correlation relationships among a large set of data items [8]. The association rules are considered interesting if they satisfy both a minimum support threshold and a minimum confidence threshold [3]. A more formal definition is the following [4]. Let I = \{i_1, i_2, ..., i_m\} be a set of items. Let D, the task-relevant data, be a set of database transactions where each transaction T is a set of items such that T \subset I. Each transaction is associated with an identifier, called TID. Let A be a set of items. A transaction T is said to contain A if and only if A \subset T. An association rule is implication of the form A \Rightarrow B, where A \subset I, B \subset I, and A \cap B = \emptyset. The rule A \Rightarrow B holds in the transaction set D with support s, where s is the percentage of transactions in D that contain A \cup B (i.e., both A and B). This is taken to be the probability, P(A \cup B). The rule A \Rightarrow B has confidence c in the transaction set D if c is the percentage of transactions in D containing A that also contain B. This is taken to be the conditional probability, P(B|A). That is, support (A \Rightarrow B) = P(A \cup B) confidence (A \Rightarrow B) = P(B | A)

The definition of a frequent pattern relies on the following considerations [5]. A set of items is referred to as an itemset (pattern). An itemset that contains k items is a k-itemset. For example the set \{name, semester\} is a 2-itemset. The occurrence frequency of an itemset is the number of transactions that contain the itemset. This is also known, simply, as the frequency, support count, or count of itemset. An itemset satisfies minimum support if the occurrence frequency of the itemset is greater than or equal to the product of minimum support and the total number of transactions in D. The number of transactions required for the itemset to satisfy minimum support is therefore referred to as the minimum support count. If an itemset satisfies minimum support, then it is a frequent itemset (frequent pattern).
The most common approach to finding association rules is to break up the problem into two parts [6]:
1. Find all frequent itemsets: By definition, each of these itemsets will occur at least as frequently as a pre-determined minimum support count [8].
2. Generate strong association rules from the frequent itemsets: By definition, these rules must satisfy minimum support and minimum confidence [8].

Additional interestingness measures can be applied, if desired. The second step is the easier of the two. The overall performance of mining association rules is determined by the first step. As shown in [2], the performance, for large databases, is most influenced by the combinatorial explosion of the number of possible frequent itemsets that must be considered and also by the number of database scans that has to be performed.

3. The Algorithms in Association Rules Mining

3.1 The Apriori Algorithm

The first pass of the algorithm simply counts item occurrences to determine the large 1-itemsets. A subsequent pass, say pass k, consists of two phases. First, the large itemsets Lk-1 found in the (k-1)th pass are used to generate the candidate itemsets Ck, using the Apriori candidate generation function (apriori-gen) described below. Next, the database is scanned and the support of candidates in Ck is counted. The Apriori algorithm is:

\[
\begin{align*}
L_1 & = \{ \text{large 1-itemsets} \}; \\
\text{for} \ (k = 2; L_{k-1} \neq \emptyset; k++ ) \ \text{do begin} \\
C_k & = \text{apriori-gen}(L_{k-1}); //\text{New candidates} \\
\text{forall} \ \text{transactions} \ t \in D \ \text{do begin} \\
C_t & = \text{subset}(C_k, t); \ //\text{Candidates contained in } t \\
\text{forall} \ \text{candidates} \ c \in C_t \ \text{do} \\
c.\text{count} & +=; \\
\text{end} \\
L_k & = \{ c \in C_k \ | \ c.\text{count} \geq \text{minsup} \} \\
\text{end} \\
\text{Answer} & = \bigcup_k L_k;
\end{align*}
\]

The apriori-gen function takes as argument Lk-1, the set of all large (k-1)-itemsets.

It returns a superset of the set of all large k-itemsets and is described in [1].

3.2 The FP-growth Algorithm

As shown in [2], the main bottleneck of the Apriori-like methods is at the candidate set generation and test. This problem was dealt with by introducing a novel, compact data structure, called frequent pattern tree, or FP-tree then based on this structure an FP-tree-based pattern fragment growth method was developed, FP-growth. This method doesn’t require candidate generation, but stores in an efficient novel structure, an FP-tree (a Frequent Pattern tree, a version of a prefix tree), the transaction database. It scans the database once to find frequent items. Frequent items F are then sorted in descending support count and kept in a list L. Another scan of the databases is then performed, and for each transaction: infrequent items are suppressed and the remaining items are sorted in L-order and inserted in the FP-tree.

**Definition 1 (FP-tree)** A frequent pattern tree is a tree structure defined below.

1. It consists of one root labeled as “root”, a set of item prefix sub-trees as the children of the root, and a frequent-item header table.
2. Each node in the item prefix sub-tree consists of three fields: item-name, count, and node-link, where item-name registers which item this node represents, count registers the number of transactions represented by the portion of the path reaching this node, and node-link links to the next node in the FP-tree carrying the same item-name, or null if there is none.
3. Each entry in the frequent-item header table consists of two fields, (1) item-name and (2) head of node-link, which points to the first node in the FP-tree carrying the item-name.

The actual algorithm, according also to [2] is:

**Algorithm 1 (FP-tree construction)**

**Input:** A transactional database DB and a minimum support threshold \( \xi \).

**Output:** Its frequent pattern tree, FP-tree

**Method:** The FP-tree is constructed in the following steps:
1. Scan the transaction database DB once. Collect the set of frequent items F and their supports. Sort F in support descending order as L, the list of frequent items.
2. Create the root of an FP-tree, T, and label it as “root”. For each transaction Trans in DB do the following.
   a. Select and sort the frequent items in Trans according to the order of L. Let the sorted frequent item list in Trans be [p | P], where p is the first element and P is the remaining list. Call insert_tree([p | P], T).
   b. The function insert_tree([p | P], T) is performed as follows. If T has a child N such that N.item-name = p.item-name, then increment N’s count by 1; else create a new node N, and let its count be 1, its parent link be linked to T, and its node-link be linked to the nodes with the same item-name via the node-link structure. If P is nonempty, call insert_tree(P, N) recursively.

The FP-growth [2] algorithm for mining frequent patterns with FP-tree by pattern fragment growth is:

**Input:** a FP-tree constructed with the above mentioned algorithm;

\( D \) – transaction database;

\( s \) – minimum support threshold.

**Output:** The complete set of frequent patterns.

**Method:**

call FP-growth(FP-tree, null).

Procedure FP-growth(Tree, A)
{ 
    if Tree contains a single path P 
    then for each combination (denoted as B) of the 
    nodes in the path P do 
    generate pattern B U A with support=minimum 
    support of nodes in B 
    else for each ai in the header of the Tree do 
    { 
    generate pattern B = ai U A with support = 
    ai.support;
    construct B’s conditional pattern base and B’s 
    conditional FP-tree
    TreeB;
    if TreeB ≠ Ø 
    then call FP-growth(TreeB, B) 
    }

4. COMPARATIVE STUDY

The following data has been processed both by Apriori 
and FP growth algorithms and they were compared. Min- 
support 50% and Min-confidence 80%.

Table 1:

<table>
<thead>
<tr>
<th>TID</th>
<th>DATE</th>
<th>ITEMS BOUGHT</th>
</tr>
</thead>
<tbody>
<tr>
<td>T100</td>
<td>10/15/99</td>
<td>K,A,D,B</td>
</tr>
<tr>
<td>T200</td>
<td>10/15/99</td>
<td>D,A,C,E,B</td>
</tr>
<tr>
<td>T300</td>
<td>10/19/99</td>
<td>C,A,B,E</td>
</tr>
<tr>
<td>T400</td>
<td>10/22/99</td>
<td>B,A,D</td>
</tr>
</tbody>
</table>

Apriori algorithm

There are two processes to find out all the large itemsets 
from the database in Apriori algorithm. First the 
candidate itemsets are generated, then the database is 
scanned to check the actual support count of the 
corresponding itemsets. During the first scanning of the 
database the support count of each item is calculated and 
the large 1-itemsets are generated by pruning those 
itemsets whose supports are below the pre-defined 
threshold. In each pass only those candidate itemsets that 
include the same specified number of items are generated 
and checked. The candidate k-itemsets are generated after 
the (k-1)th passes over the database by joining the 
frequent k-1-itemsets. All the candidate k-itemsets are 
pruned by check their sub (k-1)-itemsets, if any of its sub 
(k-1)-itemsets is not in the list of frequent (k-1)-itemsets, 
this k-itemsets candidate is pruned out because it has no 
hope to be frequent according the Apriori property. The 
Apriori property says that every sub (k-1)-itemsets of the 
frequent k-itemsets must be frequent.

Table 2 :PASS 1 
Candidate C1

<table>
<thead>
<tr>
<th>Itemset</th>
<th>Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>4</td>
</tr>
<tr>
<td>B</td>
<td>4</td>
</tr>
</tbody>
</table>

Table 3: Frequent item set L1

<table>
<thead>
<tr>
<th>Itemset</th>
<th>Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>4</td>
</tr>
<tr>
<td>B</td>
<td>4</td>
</tr>
<tr>
<td>C</td>
<td>2</td>
</tr>
<tr>
<td>D</td>
<td>3</td>
</tr>
<tr>
<td>E</td>
<td>2</td>
</tr>
</tbody>
</table>

Table 4: PASS 3 C3

<table>
<thead>
<tr>
<th>ITEM</th>
<th>COUNT</th>
</tr>
</thead>
<tbody>
<tr>
<td>{A,B,C}</td>
<td>2</td>
</tr>
<tr>
<td>{A,B,D}</td>
<td>3</td>
</tr>
<tr>
<td>{A,B,E}</td>
<td>2</td>
</tr>
<tr>
<td>{A,C,D}</td>
<td>1</td>
</tr>
<tr>
<td>{A,C,E}</td>
<td>2</td>
</tr>
<tr>
<td>{A,D,E}</td>
<td>1</td>
</tr>
<tr>
<td>{B,C,D}</td>
<td>1</td>
</tr>
<tr>
<td>{B,C,E}</td>
<td>2</td>
</tr>
<tr>
<td>{B,D,E}</td>
<td>1</td>
</tr>
</tbody>
</table>

Table 5: PASS II C2

<table>
<thead>
<tr>
<th>ITEM</th>
<th>COUNT</th>
</tr>
</thead>
<tbody>
<tr>
<td>{A,B}</td>
<td>4</td>
</tr>
<tr>
<td>{A,C}</td>
<td>2</td>
</tr>
<tr>
<td>{A,D}</td>
<td>3</td>
</tr>
<tr>
<td>{A,E}</td>
<td>2</td>
</tr>
<tr>
<td>{B,C}</td>
<td>2</td>
</tr>
<tr>
<td>{B,D}</td>
<td>3</td>
</tr>
<tr>
<td>{B,E}</td>
<td>2</td>
</tr>
<tr>
<td>{C,D}</td>
<td>1</td>
</tr>
<tr>
<td>{C,E}</td>
<td>2</td>
</tr>
<tr>
<td>{D,E}</td>
<td>1</td>
</tr>
</tbody>
</table>

Table 6: L3 

<table>
<thead>
<tr>
<th>ITEM</th>
<th>COUNT</th>
</tr>
</thead>
<tbody>
<tr>
<td>{A,B,D}</td>
<td>3</td>
</tr>
<tr>
<td>{A,B,E}</td>
<td>2</td>
</tr>
<tr>
<td>{A,C,E}</td>
<td>2</td>
</tr>
</tbody>
</table>

Table 7: L2 

<table>
<thead>
<tr>
<th>ITEM</th>
<th>COUNT</th>
</tr>
</thead>
<tbody>
<tr>
<td>{A,B}</td>
<td>4</td>
</tr>
<tr>
<td>{A,C}</td>
<td>2</td>
</tr>
<tr>
<td>{A,D}</td>
<td>3</td>
</tr>
<tr>
<td>{A,E}</td>
<td>2</td>
</tr>
<tr>
<td>{B,C}</td>
<td>2</td>
</tr>
<tr>
<td>{B,D}</td>
<td>3</td>
</tr>
<tr>
<td>{B,E}</td>
<td>2</td>
</tr>
<tr>
<td>{C,E}</td>
<td>2</td>
</tr>
</tbody>
</table>

The last table L3 gives the frequent item set with 
minimum support 50%.
Confidence :
Suppose we take any one of the frequent item say {A,B,D}
The possible association rules are given by
AAB⇒D IS ¾ WHICH IS 75%
AAD⇒B IS 3/3 WHICH IS 100%
BAD⇒A IS 3/3 WHICH IS 100%
D⇒AAB IS 3/3 WHICH IS 100%
B⇒AAD IS 3/4 WHICH IS 75%
A⇒BAD IS 3/4 WHICH IS 75%
Since the given level of confidence is 80% the bolded associations rules are stronger.

FP growth tree algorithm :

CONSTRUCTION OF FP TREE
The process of constructing the FP-Tree is as follows.
(1) The database is scanned for the first time, during this scanning the support count of each items are collected. As a result the frequent 1 -itemsets are generated as shown , this process is the same as in Apriori algorithm. Those frequent itemsets are sorted in a descending order of their supports. Also the head table of ordered frequent 1 -itemsets is created .

<table>
<thead>
<tr>
<th>Itemset</th>
<th>Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>4</td>
</tr>
<tr>
<td>B</td>
<td>4</td>
</tr>
<tr>
<td>D</td>
<td>3</td>
</tr>
<tr>
<td>C</td>
<td>2</td>
</tr>
<tr>
<td>E</td>
<td>2</td>
</tr>
</tbody>
</table>

TABLE 8: ORDERED LIST L1

(2) Create the root node of the FP-Tree T with a label of Root. The database is scanned again to construct the FP-Tree with the head table, for each transaction the order of frequent items is resorted according to the head table. For example, the first transaction (K;A;D;B) is transformed to (A;B;D;K), since A occurs more frequently than other items in the database. Let the items in the transaction be [p j P], where p is the first frequent item and P is the remaining items list, and call the function Insertj[p j P];
(3) The function Insertj[p j P]; works as follows. If T has a child N such that N.item-name=p.item-name then the count of N is increased by 1, else a new node N is created and N.item-name=p.item-name with a support count of 1. Its parent link be linked to T and its node link is linked to the node with the same item-name via a sub-link. This function InsertjFP:Tg is called recursively until P becomes empty.

Let's take the insertion of first transaction to the FPTree as an example to illustrate the insert function and construction of FPTree we mentioned above. After reoder this transaction is (A; B;D;K), so p is A in this case, while P is (B;D;K). Then we call the function of insert, first we search and determine the node A exists in the tree or not, it turns out A is a new node. According to the rules, a new node named A is created with a support count of 1. Since here T is Root, node A is linked to Root and call the insert function again. At this time p is B, P is (D;K), T is A.The result of the FPTree of the database is shown.

Figure 1: Mining FP tree

Table 9: mining of FP tree

<table>
<thead>
<tr>
<th>Item</th>
<th>Conditional pattern</th>
<th>Condition FP tree</th>
<th>Frequency pattern generated</th>
</tr>
</thead>
<tbody>
<tr>
<td>E</td>
<td>(ABDC:1),(ABC:1)</td>
<td>ABC:2</td>
<td>ABCE:2</td>
</tr>
<tr>
<td>D</td>
<td>(BA :3)</td>
<td>BA :3</td>
<td>BAD:3</td>
</tr>
<tr>
<td>C</td>
<td>ABD:1,AB:1</td>
<td>AB:2</td>
<td>ABD:2</td>
</tr>
<tr>
<td>B</td>
<td>A:4</td>
<td>A:4</td>
<td>AB:4</td>
</tr>
</tbody>
</table>

Mining of the FP tree is summarized in the above table. Let us first consider the last item in the ordered list that is K.K occurs in one branch of the tree that is ABDK: 1. Considering K as suffix its corresponding path is ABD: 1. Since it 's support count does not satisfy the condition of minimum support it is not included in the conditional pattern. For the next data E it’s two paths are ABDC: 1,ABC : 1 which generates conditional FP tree ABC:2 and derives frequent item pattern as ABCE:2.

In Apriori algorithm to find a frequent k-itemset it requires k passes over the database. Frequent itemsets of over 50-60 items are not feasible. Apriori avoids the effort wastage of counting the candidate itemsets that are known to be infrequent. The candidates are generated by joining among the frequent itemsets level-wisely, also candidate are pruned according the Apriori property. As a result the number of remaining candidate itemsets ready for further support checking becomes much smaller, which dramatically reduces the computation, I/O cost and memory requirement.

There are two bottlenecks of the Apriori algorithm. One is the complex candidate generation process that uses most of the time, space and memory. Another bottleneck is the multiple scan of the database.

Frequent pattern mining is another milestone in the development of association rule mining, which breaks the two bottlenecks of the Apriori. The frequent itemsets are
generated with only two passes over the database and without any candidate generation process. FP-Tree was introduced by Han et al. [Han et al. 2000]. By avoiding the candidate generation process and less passes over the database, FP-Tree is an order of magnitude faster than the Apriori algorithm. The frequent patterns generation process includes only two sub processes: constructing the FT-Tree, and generating frequent patterns from the FP-Tree.

The efficiency of FP-Tree algorithm account for three reasons. First the FP-Tree is a compressed representation of the original database because only those frequent items are used to construct the tree, other irrelevant information are pruned. Also by ordering the items according to their support the overlapping parts appear only once with different support count. Secondly this algorithm only scans the database twice. The frequent patterns are generated by the FP-growth procedure, constructing the conditional FP-Tree which contain patterns with specified suffix patterns, frequent patterns can be easily generated as shown in above the example. Also the computation cost decreased dramatically. Thirdly, FP-Tree uses a divide and conquer method that considerably reduced the size of the subsequent conditional FP-Tree, longer frequent patterns are generated by adding a suffix to the shorter frequent patterns. In [Han et al. 2000] [Han and Pei 2000] there are examples to illustrate all the detail of this mining process.

The number of disk access is critical in data mining task, because the I/O operation is more time consuming than a memory operation. It can be of advantage when we minimize the disk access. The level wise algorithms (Apriori) read the whole database k times for finding the k-frequent itemset. The algorithm will read the database as many times, as long the longest itemset is. If there is only one long frequent itemset, the mining time will increase rapidly.

The two-phase mining algorithms (FP tree) read the database only twice. In one case by the first database reading the support count of the 1-frequent itemsets are determined, and using this information reading the second time the database we can build the whole database in the memory with a clever compression of the database. The mining operation has to be accomplished only in the memory.

Every algorithm has his limitations, for FP-Tree it is difficult to be used in an interactive mining system. During the interactive mining process, users may change the threshold of support according to the rules. However for FP-Tree the changing of support may lead to repetition of the whole mining process. Another limitation is that FP-Tree is that it is not suitable for incremental mining. Since as time goes on databases keep changing, new datasets may be inserted into the database, those insertions may also lead to a repetition of the whole process if we employ FP-Tree algorithm. Regarding the I/O cost, it is a very essential parameter, how many times the algorithm accesses the database.

5. CONCLUSION

From the experimental data presented it can be concluded that the FP-growth algorithm behaves better than the Apriori algorithm. First of all, the FP-growth algorithm needs at most two scans of the database, while the number of database scans for the candidate generation algorithm (Apriori) increases with the dimension of the candidate itemsets. Also, the performance of the FP-growth algorithm is not influenced by the support factor, while the performance of the Apriori algorithm decreases with the support factor.

Thus, the candidate generating algorithms (derived from Apriori) behave well only for small databases (max. 50,000 transactions) with a large support factor (at least 30%). In other cases the algorithms without candidate generation FP-growth behave much better.

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REFERENCES


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